OPTIMAL DESIGN OF FRACTION-ORDER PROPORTIONAL-DERIVATIVE PROPORTIONAL-INTEGRAL CONTROLLER FOR LFC OF THERMAL-THERMAL-WIND TURBINES CONSIDERING NONLINEARITIES

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Abstract: The power system must be kept safe during load disturbances in order to control frequency instability during load disturbances change. Cascade Controller (CC) is employed to boost the performance of the power system mainly in the presence of nonlinear aspects. As a result, in this study, A proposed cascade fractional order proportional-derivative proportional integral (FOPDPI) controller is used to fine-tune the load frequency control (LFC) subjects of a three-area power system (thermal-thermal-wind) in the interconnected power system (IPS). As a third area in the studied model, renewable energy is used, such as high penetrating power wind turbines. The FOPDPI controller gains are adjusted using a recently published optimization scheme, such as the Harris hawk optimizer (HHO). To thoroughly test the efficiency and fitness of the proposed controller, the HHO-based FOPDPI and conventional PID controllers are applied to a three-area model with/without nonlinearities such as generation rate constraint (GRC), governor dead band (GDB), and boiler dynamics (BD) under different step load perturbation (SLP). The HHO algorithm’s cost function is the Integral time multiply absolute error (ITAE) criterion. The investigation reveals that the proposed scheme HHO: FOPDPI provides greater stability than HHO: PID in both linearities by 58% and nonlinearity aspects by 62%.

Keywords: Cascade controller; load frequency control; Harris hawks’ algorithm; and fraction order PID controller.

1. Introduction

Electricity production should be in line with consumer demands; to control frequency and voltage instability, the system must be saved during load disruptions, [1]. LFC is required in the power system to maintain nominal tie-line power and system frequency during any disturbance. The area control error (ACE) is the LFC’s regulated output, which is forced to zero to eliminate frequency and tie-line power deviations. [2]. Numerous LFC methods, such as proportional-integral (PI) LFC, have been developed to maintain tie-line power and system frequency at default parameters under both normal and disrupted conditions [3], dual-mode PI control [4] integral derivative (ID) [5] for LFC issues are also presented. The PID and optimal PID controllers are employed for LFC issues are presented in [6] and [7], respectively. In [8], a multi-area LFC is introduced Properly tuning the parameters for the aforementioned schemes necessitates a more thorough examination of their robustness in the face of the uncertainties. [9]. Soft-computing-based control methods, such as genetic algorithm (GA), [10], particle swarm optimization (PSO), [11] are used to improve performance because they provide a reasonable solution to issues such as nonlinearities, uncertainties, and complexity in the LFC. Several recent schemes have been technologically advanced to address LFC problems in traditional and existing power systems based PID controller, such as the bacterial foraging optimization (BFO) [12], differential evolution (DE), [13], teaching-learning-based optimization (TLBO), [14]. To address the LFC issues, a new fraction order PID (FOPID) controller is proposed, [15]. Also, a cascade fuzzy plus FOPID controller for two-area power system is presented in [16].

The efficiency of non-cascade controllers has greatly degraded, due to rising power system complexities such as boiler dynamics, delay in time,
dead band, heavy load disruptions and other nonlinearities. The Cascade Control (CC) mechanism is one of the powerful controls that can efficiently be used to improve the efficiency of the control system, [17]. Therefore, The cascade PID-PID controller is used to preserve the ACE at steady state action is presented in [18]. Also, in [19], maiden application of cascade tilt-integral-derivative (TID) controller in LFC is presented. The ongoing evolution of controller structures and computer algorithms gives researchers great inspiration for applying the new ones to find the best possible solutions to LFC problems in order to achieve an increased degree of smooth, damp oscillation in power system intermediates. The HHO is a revolutionary system of optimization influenced by Harris' cooperative behavior and chasing style, called a surprise blow, [20]. HHO can be extended to various technical problems because of its balance between the exploration and exploitation phases and simplicity for tuning one parameter used defined, [21], [22]. In the IPS, the HHO is also applied, where the design of cascade FO-PID/PID controller for speed control of DC motor is employed, [23].

From the above discussion, the enhancement of the IPS operation comes from: fractional order controller, cascade controller, and a powerful optimization algorithm. Therefore, in this paper, CC from FOPID and its pertinent are used. In this paper, a mixture of the HHO based a cascade FOPDPI controller under ITAE cost function is proposed. The HHO based FOPDPI and PID controllers are used as additional controls to investigate the LFC in a two-phases environment. The first case is to implement the power system model without nonlinearity, as well as renewable energy systems such as wind power turbines, as a third area. The second stage is then to incorporate the nonlinear model with GRC, BD and GDB to demonstrate the efficiency and robustness of the FOPDPI controller system and to improve the system stability by approximately 60% compared to the traditional PID.

This paper will be reset accordingly. Section 2 demonstrates the proposed power system and the FOPDPI controller design under ITAE criterion. Section 3 describes the HHO algorithm. Section 4 presents the simulation results and discussion. Finally, section 5 accomplishes the work.

2. System design

2.1 Modelling of Power system

In this segment, the IPS of three-area (Thermal-Thermo-Wind turbines) is presented. This model consists of more actual sources, including a thermal unit, area 1, thermal unit, area two and a wind unit, area three. The suggested transfer functions of the power grid are shown in Fig. 1.

![Transfer Function of the Three-Area Thermal-Thermal-Wind Power System with Reheater Including BD, GRC and GDB Nonlinearities](image-url)
The suitable parameters of the studied power system are reflected as in [24], as displayed in Appendix A. The system strategy studies non-linearities, such as the GDB [25], BD [26] as shown in Fig. 2, and the oscillation produced due to GDB is sinusoidal in nature and has a time-period of 2s. In this work, GDB considered for the thermal system are 0.05%, [27]. The GRC of 3% per minute is considered in a thermal plant.

2.2 Controller structure

The basic PID controller and its related derivatives are commonly used in engineering problems because of its basic design, structural simplicity, a satisfactory relationship between cost and efficiency, lower demands on user skill, low cost, and productivity. The FOPID controller is now widely used for LFC problems as an additional controller. The FOPID structure is shown in Fig. 3(a). The CC construction is based on two successive operations in which internal operation (FOPD) is the sequence of external function (FOPI) as structured in Fig. 3(b).

The CC’s main goals include: The internal mechanism attenuates the effect of supply interruption as the external process manages the final control signal of output [28]. A CC system can quickly reject a disturbance until it spreads to other components of the process to attain better performance [24].

2.3 Cost/Objective function

LFC needs to achieve two goals under load disturbances: to restore steady-state frequency to zero and to maintain the transmitted power at pre-detailed values. LFC should therefore be carefully calibrated to the most appropriate goal role. The integrated multiplied absolute error (ITAE) is the main objective criterion for the LFC specification, [14]. The value reduction of the objective function given by ITAE verifies the optimization as follows:

\[
J = \int_0^{t_{sim}} (|\Delta F_i| + |\Delta P_{tie-i}|) \cdot t \cdot dt \quad (1)
\]

where \( t_{sim} \) is the simulation time; \( \Delta F \) is the frequency deviation, \( P_{tie} \) is the tie-line power deviation, \( i \) stands for area 1,2, and 3. The controller gains subject to:

\[
K_{x_{\min}} \leq K \leq K_{x_{\max}} \quad (2)
\]

where \( x \) can denote \( k_{p1}, k_D \) and \( K_{p2}, K_i \) of the FOPD and FOPI gains, respectively. \( K_{x_{\min}} \) and \( K_{x_{\max}} \) are the lower and upper values within [0, 2] range and \( \mu \) and \( \lambda \) within [0, 1] of the working FOPDPI controller gains, [29],[30].

3. Harris Hawks Algorithm

The Harris Hawks Algorithm (HHO) comes as a source of collaboration called a surprise punch. In this tactic, several hawks combine together to provoke the prowess in several ways. HHO’s stalking habits and patterns of prey escape are the product of dynamic nature scenarios. HHO is based on population number and can be used for any optimization problem without gradient optimization. HHO phases are explained in the following subsections.

3.1 Exploration stage
Two main proposals are focused on Harris Hawks detecting prey.

\[
X(t+1) = \begin{cases} 
X_{\text{rand}}(t) - r_1 | X_{\text{rand}}(t) - 2r_2 X(t) |, & q \geq 0.5, \\
(X_{\text{prey}}(t) - X_m(t)) - r_3 (LB + r_4 (UB - LB)), & q < 0.5
\end{cases}
\]  

(3)

where \(X(t+1)\) is the hawks site in the succeeding iteration \(t\); \(X_{\text{prey}}(t)\) is the prey position, \(X(t)\) is the hawks current location of \((q), r_1, r_2, r_3,\) and \(r_4\) are random numbers within \([0, 1]\), UB and LB are the upper and lower boundary variables, \(X_{\text{rand}}(t)\) is a randomly selected hawk from the current population, and \(X_m\) is the average location of the hawks is denoted by:

\[
X_m(t) = \frac{1}{N} \sum_{i=1}^{N} X_i(t) \tag{4}
\]

where \(X_i(t)\) specifies the location of each hawk and \(N\) is the total number of hawks. To convert from the exploration phase to exploitation phase, the prey energy is exhibited as:

\[
E = 2E_0 \left(1 - \frac{t}{T}\right) \tag{5}
\]

where \(E\) is the prey fleeing energy, \(T\) is the cumulative number of iterations performed, and \(E_0\) is initial energy of the prey.

### 3.2 Exploitation stage

depending on the value of \(|E|\) compared to 0.5, the soft and hard blockade occurs happens.

a) **Soft blockade**

When \(r \geq 0.5\) and \(|E| \geq 0.5\), this behavior is exhibited by:

\[
X(t+1) = \Delta X(t) - E|JX_{\text{prey}}(t) - X(t)| \tag{6}
\]

\[
\Delta X(t) = X_{\text{prey}}(t) - X(t) \tag{7}
\]

where \(X(t)\) is the remoteness between the prey position and the current hawk position, \(r_5\) is a random number within \([0,1]\), and \(J = 2(1 - r_5)\) signifies the prey jump strength through in the escaping process.

b) **Hard blockade**

Aspired When \(r \geq 0.5\) and \(|E| < 0.5\), and the locations are updated by:

\[
X(t+1) = X_{\text{prey}}(t) - E|\Delta X(t)| \tag{8}
\]

c) **Soft rapid dives**

Inputs: Set the max. No. of Iterations, the population size, upper and lower boundary, and the No. of variables.

Outputs: the location of prey and its fitness value.

While stopping condition is not met do

Compute the fitness value of Hawks

Set \(X_{\text{prey}}\) as the location of prey (best solution)

For each hawk do

Update the initial energy and the jump strength \(J\)

Update the energy using Eq. (5)

If \(|E|\geq 1\) then

Update the position vector using Eq. (3)

else if \((r \geq 0.5\) and \(|E| \geq 0.5\)) then

Update the position vector using Eq. (6)

else if \((r < 0.5\) and \(|E| \leq 0.5\)) then

Update the position vector using Eq. (8)

else if \((r < 0.5\) and \(|E| < 0.5\)) then

Update the position vector using Eq. (12)

else if \((r < 0.5\) and \(|E| < 0.5\)) then

Update the position vector using Eq. (13)

Return \(X_{\text{prey}}\)

It happened When \((r < 0.5\) and \(|E| \geq 0.5\)). On the basis of next norm, the hawks will decide their next action:

\[
Y = X_{\text{prey}}(t) - JX_{\text{prey}}(t) - X(t) \tag{9}
\]

We theorized that they would jump based on LF:

\[
Z = Y + S \times LF(D) \tag{10}
\]

where \(D\) is the problem dimensions and \(S\) is a random vector size and \(LF\) is the levy flight function, which is estimated as follows:

\[
LF(X) = 0.01 \times \frac{u \times \sigma}{|v|^\beta} \tag{11}
\]

Where \(\sigma\) is the variance of Brownian random walks [20]; \(u, v\) are random values within \([0, 1]\), \(\beta\) is a constant equal to 3/2. Hence, the concluding strategy for positions updating of hawks in the soft blockade stage can be achieved by

\[
X(t+1) = \begin{cases} 
Y, & \text{if } F(Y) < F(X(t)), \\
Z, & \text{if } F(Z) < F(X(t))
\end{cases} \tag{12}
\]
where $Y$ and $Z$ are obtained using Eqs. (13) and (14).

d) **Hard rapid dives**

When $|E| < 0.5$ and $r < 0.5$, hard progressive transpire and hawks’ position are attained by:

$$X(t + 1) = \begin{cases} Y, & \text{if } F(Y) < F(X(t)), \\ Z, & \text{if } F(Z) < F(X(t)) \end{cases}$$  \hspace{1cm} (13)

where $Y$ and $Z$ are estimated by:

$$Y = X_{\text{prey}}(t) - |JX_{\text{prey}}(t) - X_m(t)|$$  \hspace{1cm} (14)

$$Z = Y + S \times LF(D)$$  \hspace{1cm} (15)

The pseudocode of HHO algorithm is demonstrated in Fig. 4.

### 4. Simulation Results and discussion

The studied model is performed in the MATLAB/SIMULINK (2017b) environment operational on Intel, core i – 5, 2.3 GHz and 8 GB RAM. The HHO scheme and the objective function (ITAE) criterion are written (.m file). The proposed HHO: FOPDPI controller is modelled with the FOMCON toolbox, a fractional-order calculus-based toolbox for system modelling and control design with 0.001 step time. For efficient system performance, population of HHO algorithm should be selected prudently, consequently the optimization procedure is performed 15 times with different population number to typically select the best gains for FOPDPI controller parameters. The best selection of population number is 60. The system is inspected with and without the nonlinearity under FOPDPI and PID controllers. The proposed HHO: FOPDPI scheme under ITAE criterion is implemented. The FOPDPI and PID controller gains with and without the nonlinearity are exposed in Table 1.

Fig. 5 and Fig.6 show the dynamic response of HHO based FOPDPI and PID controllers under a 1% and 5% SLP in area 1, respectively. Fig. 5a, 6a, 5b, 6b and 5c, 6c show the deviation in frequency in area 1 ($\Delta F_1$), area 2 ($\Delta F_2$), and area 3 ($\Delta F_3$), respectively. The tie-line power deviations are shown in Figs. 5d, 6d, 5e, 6e, and 5f, 6f for $\Delta P_{\text{tie}-12}$, $\Delta P_{\text{tie}-13}$, and $\Delta P_{\text{tie}-23}$, respectively. From these Figures the proposed controller FOPDPI is more effective than the PID controller in both the settling time and deviations peaks. The step load disturbance is increased to 5% to deeply check the stability of the proposed HHO/FOPDPI controller as shown on Fig. 6. The dynamic response parameters in terms of overshoots, undershoots and the settling time are increased adequately, and the system is a sufficiently stable which demonstrates the robustness of the proposed HHO/FOPDPI scheme.

The table below shows the optimized PID and FOPDPI Controllers Gains.

<table>
<thead>
<tr>
<th>HHO: FOPDPI</th>
<th>Linear model</th>
</tr>
</thead>
<tbody>
<tr>
<td>Area 1</td>
<td>Area 2</td>
</tr>
<tr>
<td>$K_{F1}$</td>
<td>1.9896</td>
</tr>
<tr>
<td>$K_{D}$</td>
<td>2.0000</td>
</tr>
<tr>
<td>$K_{P2}$</td>
<td>1.9958</td>
</tr>
<tr>
<td>$K_{I}$</td>
<td>2.0000</td>
</tr>
<tr>
<td>$\mu$</td>
<td>0.7355</td>
</tr>
<tr>
<td>$\lambda$</td>
<td>0.9178</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>HHO: PID</th>
<th>Linear model</th>
</tr>
</thead>
<tbody>
<tr>
<td>Area 1</td>
<td>Area 2</td>
</tr>
<tr>
<td>$K_{P1}$</td>
<td>2.0000</td>
</tr>
<tr>
<td>$K_{D}$</td>
<td>0.3269</td>
</tr>
<tr>
<td>$K_{P2}$</td>
<td>0.0601</td>
</tr>
<tr>
<td>$K_{I}$</td>
<td>1.9773</td>
</tr>
<tr>
<td>$\mu$</td>
<td>0.6984</td>
</tr>
<tr>
<td>$\lambda$</td>
<td>1.0000</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>HHO: PID</th>
<th>Including nonlinearities</th>
</tr>
</thead>
<tbody>
<tr>
<td>Area 1</td>
<td>Area 2</td>
</tr>
<tr>
<td>$K_{P1}$</td>
<td>2.0000</td>
</tr>
<tr>
<td>$K_{D}$</td>
<td>0.0000</td>
</tr>
<tr>
<td>$K_{P2}$</td>
<td>0.9708</td>
</tr>
<tr>
<td>$K_{I}$</td>
<td>0.7391</td>
</tr>
<tr>
<td>$\mu$</td>
<td>1.5742</td>
</tr>
<tr>
<td>$\lambda$</td>
<td>0.5697</td>
</tr>
</tbody>
</table>

The effect of the nonlinearities such as GRC, BD and GDB have a bad effect at the frequency deviations and tie-lines power deviations. The settling time of FOPDPI controller is highly increased, but it is provided a more stability than PID controller. The ITAE value in the linearity phase of FOPDPI is (0.051) 1% SLP while in nonlinearity option the ITAE value is increased to (4.764) under 2% SLP compared to PID where ITAE is (0.1567) without nonlinearities under 1% SLP and (24.642) with nonlinearities under 2% SLP. The nonlinearity aspects have a great effect at the stability of the power system, but the proposed HHO based FOPDPI has a great stability as shown in Fig. 7. The minimum undershoot is the frequency deviation in area-2 (0.02715) which demonstrate the effectiveness of the proposed controller.
5. Conclusion

In this study, the optimally tuned FOPDPI and PID controllers using the ITAE objective functions with and without nonlinearities are presented using a recent novel HHO algorithm to obtain more practical results for the LFC study and to demonstrate the intensity of the proposed FOPDPI controller. A model of three area one-unit of thermal-thermal-wind power plants is studied. Firstly, the model is studied without nonlinearities to check the suitability of the proposed HHO: FOPDPI scheme in dealing with LFC issues compared to HHO: PID at the same environment. The investigation model's dynamic LFC response profiles for the interconnected power system are presented. Because it has small-magnitude oscillations, the time-domain investigation verifies the stability output of the FOPDPI cascade controller in both cases: linearity under 1% and 5% SLP and the non-linearity process, including the GRC, BD, and GDB under 2% SLP. The investigation results disclose that the proposed HHO tuned FOPDPI cascade controller has been demonstrated to make the LFC system resilient and to provide a stable and better outcome under a wide range of nonlinearity conditions than conventional PID controller.
Fig. 5 Transient responses of the system under 5% SLP in area 1. (a) $\Delta F_1$, (b) $\Delta F_2$, (c) $\Delta F_3$, (d) $\Delta P_{tie12}$, (e) $\Delta P_{tie23}$, (f) $\Delta P_{tie13}$. 
Appendix [31]

\[
B_1 = B_2 = B_3 = B = 0.425 \text{ p.u.}; \quad R_1 = R_2 = R_3 = R = 2.4\text{Hz/p.u.}; \quad T_{t1} = T_{t2} = T_{t3} = T_{t23} = 0.086; \quad a_{12} = a_{13} = a_{23} = -1; \quad T_{g1} = T_{g2} = 0.08 S; \quad K_{P1} = K_{P2} = K_{P3} = K_{P5} = 120\text{Hz/p.u.}; \quad T_{p1} = T_{p2} = T_{p3} = T_{p3} = 10S; \quad T_{P1} = 6 s; T_{P2} = 0.041 s; \quad K_{P1} = 1.25; \quad K_{P2} = 1.4.
\]

Parameters of BD:

\[
K_1 = 0.85; \quad K_2 = 0.095; \quad K_3 = 0.92; \quad K_{ib} = 0.03; \quad r_{ib} = 26; \quad T_{ib} = 69; \quad T_{rb} = 6.9; \quad C_B = 200; \quad T_D = 0; \quad T_f = 10 s.
\]

References


